

Question #1: Determine the continuous-time Fourier transform (CTFT) or inverse CTFT for the following equations. Use the continuous-time transform tables on the course website.

(a) $x(t) = u(t + 2) - u(t - 2)$

Solution:

$$X(\Omega) = 4 \operatorname{sinc}(2\Omega)$$

(b) $x(t) = u(t) - u(t - 4)$

Solution:

$$X(\Omega) = 4 \operatorname{sinc}(2\Omega) e^{-j\Omega 2}$$

(c) $x(t) = e^{-t} u(t - 1) * e^{-2t} u(t)$

Solution:

$$\begin{aligned} x(t) &= e^{-(t-1)-1} u(t-1) * e^{-2t} u(t) \\ &= e^{-1} e^{-(t-1)} u(t-1) * e^{-2t} u(t) \\ X(\Omega) &= e^{-1} \left(\frac{e^{-j\Omega}}{1 + j\Omega} \right) \left(\frac{1}{2 + j\Omega} \right) \end{aligned}$$

(d) $X(\Omega) = j\pi [\delta(\Omega - \pi/3) - \delta(\Omega + \pi/3)]$

Solution:

$$x(t) = -\sin((\pi/3)t)$$

